

The SAS GLMCURV9 Macro

Ellen Hertzmark, Ruifeng Li, Biling Hong, and Donna Spiegelman

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Abstract

The %GLMCURV9 macro uses SAS PROC GENMOD and restricted cubic splines to test whether there is a nonlinear relation between a continuous exposure and an outcome variable. The macro can automatically select spline variables for a model. It produces a publication quality graph of the relationship.

Keywords: generalized linear models, PROC GENMOD, generalized estimating equations, GEE, nonlinearity, restricted cubic splines, automatic variable selection, graphics

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1 Description

The %GLMCURV9 macro uses SAS PROC GENMOD and restricted cubic splines to test whether there is a nonlinear relation between a continuous exposure and an outcome variable. The outcome variable can be dichotomous (binary) or continuous. The user can control the variance distribution, the link function, and the working covariance structure. The macro can automatically select spline variables for a model. It produces a publication quality graph of the relationship. It can also produce a file to use in other plotting programs.

2 Invocation and Details

Parameters with default values are listed as OPTIONAL below.

PARAMETERS RELATING TO THE DATA SET

=====

DATA=, The name of the dataset to use
REQUIRED

EXPOSURE=, The continuous variable you are testing for
nonlinearity
REQUIRED

OUTCOME=, The dependent variable.
This can be dichotomous/binary or continuous
REQUIRED

HPCT=, The percentile of the EXPOSURE at which to trim the data at the high end
If the data are highly skewed, the highest values may not
be helpful in determining what the relationship is in the
bulk of the sample.
Typically at least 95.
OPTIONAL

LPCT=, The percentile of the EXPOSURE at which to trim the data at the low end.
Similar to HPCT.
Typically at most 5
OPTIONAL

HICUT=, A value of the EXPOSURE at which to trim the data at the high end.
This may be based on biological plausibility for values of the
exposure, but you don't want to delete too much of your sample
OPTIONAL

LOWCUT=, A value of the EXPOSURE at which to trim the data at the low end.
Similar to HICUT
OPTIONAL

WHERE=, A conditional clause to restrict the analysis to a subset of the data
examples: sex eq male
 %str (age lt 75)
NOTE: No commas or = signs allowed, unless using %str
OPTIONAL

SUBJECT=,
REQUIRED if you have repeated measures.

PARAMETERS RELATED TO THE MODEL AND THE REPORT

=====

DIST=, The distribution to use.
Options are N (normal), B (binomial), P (poisson), G (gamma),
NB (negative binomial), MULT (multinomial), IG (inverse gaussian).
REQUIRED

LINK=, The link function to use.
Options are ID, LOG, LOGIT, Power(-1), Power(-2), CLOGIT
If you do not specify the LINK, the macro will use the canonical
link function for the specified distribution, and will tell you so
in a diagnostic
OPTIONAL (if you want to use the canonical link function)

ADJ=, The list of covariates in the model.
This can be written using the macro variables made by %INDIC3,
but CANNOT use notation like xq1-xq4 or xq:

OPTIONAL (i.e. crude models are allowed)

ADJDAT=, The name of the SAS dataset containing the values of the covariates at which you want to evaluate the outcome for the graph. These should usually be near the center of the distribution for each variable.
ADJDAT has one observation.
REQUIRED if there are covariates and the plot is not the odds ratio or the risk ratio (i.e. PLOTOR=F, see below)

BYVAR=, The name of a variable by which to stratify the results.
e.g. SEX, AGE GP
NOTE: If BYVAR has more than 2 values, the prediction curves will be plotted on the same graph without the confidence limits.
OPTIONAL

WEIGHTVAR=, The name of a variable in DATA to be used as a weight for the model
OPTIONAL

REFVAL=MIN, The value to use as a reference value for the splines.
Can be a user-given number or a statistic such as MIN, MAX, MEAN, MEDIAN.
OPTIONAL and not applicable for continuous outcome variables.

NK=, The number of knots to use.
Can be 3, 4, 5, 6, 7, 8, 9, 10, 17, 21, 25, 50.
If you do not give NK or KNOT (see below) and have SELECT=3, (see below), the macro will set NK=21. If SELECT is not 3, the macro will set NK=4 by default.
Among the diagnostics the macro prints out are lines stating the fractions of the data range below the lowest knot or above the highest knot. If these are above 20%, it is advisable to do one of the following: (1) trim the data using HPCT, LPCT, HICUT, or LOWCUT (as appropriate);
(2) use KNOT (see next parameter);
(3) adjust the horizontal axis so that not too much of the visible graph is beyond the last knot (see AXORDH).
and add at least one more knot location
OPTIONAL

KNOT=, a list of values of the EXPOSURE to be the knots for the splines.
IF KNOT is not null, it overrides NK
OPTIONAL

USEGEE=F, Whether you want to use the empirical variance when there is one record per subject.
USEGEE=T by default if you have any subject with more than one observation.
OPTIONAL

REPTYPE=IND, The working correlation structure to use.
IND for one observation per person;
EXCH or CS for exchangeable;
MDEP(1), MDEP(2) for Toeplitz types;
UN
REQUIRED

WITHINVAR=, If REPTYPE is not IND or EXCH, the variable that tells PROC GENMOD

the order of the observations within each SUBJECT,
REQUIRED (if REPTYPE is not IND or EXCH)

SELECT=1, Whether you want to use automatic selection to make your model.
1=No selection (i.e. use all spline variables)
If NK is large, this may result in a graph with many
unimportant/extraneous 'wiggles.'
2=Use spline variables specified by user (See USERSPLV below)
3=Use automatic selection of spline variables
OPTIONAL

USERSPLV=, If SELECT=2 and you are not using BYVAR, the list of spline variables to
include in the model.
This would normally come from a previous run of the macro
in a situation where the selection takes a lot of time and
you are just trying to improve the graph.

USERSPLV1=, Like USERSPLV for the first level of the BYVAR, if you have one
USERSPLV2=, Like USERSPLV for the second level of the BYVAR, if you have one
...
...
USERSPLV10=, Like USERSPLV for the tenth level of the BYVAR, if you have one

SLE=.05, If SELECT=3, the p-value at which a variable enters the model
OPTIONAL

SLS=.05, If SELECT=3, the p-value at which a variable leaves the model
OPTIONAL

HEADER1=, A description of the analysis
The default is GRAPHTIT (See below), and if that is empty,
OUTCOME and EXPOSURE.
OPTIONAL

TESTREP=LONG, The type of report you want for the tests of the 3
hypotheses:
1. Whether the relationship between the EXPOSURE
and the OUTCOME, if it is significant, is
nonlinear;
2. If the p-value for the first test is small, the
p-value for the overall significance of the curve
(i.e., is the nonlinear relationship significant?)
3. If the p-value for the first test is large, the
p-value for the linear relationship (i.e. is the
linear relationship significant?)
The LONG report (default) gives explicit directions
about how to read the report. The SHORT report is
more terse.
OPTIONAL

MODPRINT=T, Whether to print the results of the 3 models:
Adjusters only
Adjusters plus linear EXPOSURE
Adjusters plus linear EXPOSURE plus any splines used
(based on SELECT=1 or 2, or on automatic selection)
OPTIONAL

PVALUEFORMAT=pvalue6.4, The format for printing the p-values in the
report.

OPTIONAL

PARAMETERS RELATING TO THE GRAPH

=====

PLOT=2, The type of plot output you want:

0. No plot
1. PROC PLOT in the SAS .lst
2. Some publication-quality format
Options are PS (encapsulated postscript), PDF, JPEG, CGM (see OUTPLOT below).
3. PROC PLOT and a publication-quality format
4. Just a text file of the plotting points to use in some other plotting program

OPTIONAL

OUTPLOT=PS, The type of publication-quality format you want.

If OUTPLOT is not 2 or 3, this will be ignored.

OPTIONAL

GRAPHTIT= The title of the graph.

If no GRAPHTIT is specified, HEADER1 will be used.

IF no title is wanted (e.g. for publication), use GRAPHTIT=NONE (upper case required).

OPTIONAL

PICTNAME=&data.&exposure.&outcome.&sel&select.&nk.&outplot ,

The name of the graphics file.

We strongly suggest that you use a mnemonic name, rather than relying on the default (which can get overwritten if another macro call with the same parameters is run).

OPTIONAL

FOOTER=DEFAULT, The footnote for the graph.

The default footnote lists the first few variables in ADJ, followed by 'and other variables'.

If you want a footnote, it is more informative to make up your own.

If no footnote is desired, set FOOTER=NONE.

OPTIONAL

PLOTOR=F, Whether to plot the odds ratio or risk ratio, rather than the direct outcome of the model. Usually models with logit or log links will have PLOTOR=T, while other models will not.

OPTIONAL

CI=T, Whether to plot confidence band as cloud

If you say 'F,' the confidence band will be bounded by dot-dash curves.

OPTIONAL

PWHICH=SPLINE, Whether to plot the spline graph or the linear graph.

It is not usually of interest to plot the linear graph if the relationship is not nonlinear,

OPTIONAL

DISPLAYX=T Whether to show the smoothed histogram of the EXPOSURE

OPTIONAL

VLABEL= The label for the vertical axis.
 Be specific. Give a human-interpretable label with units, if appropriate (e.g. Predicted BMI (kg per sq m), or %str(Predicted BMI (kg/sq. m))).
 If PLOTOR=T, Predicted Odds Ratio (or Predicted Risk Ratio) for {some human-interpretable description of the outcome}
 OPTIONAL

AXORDV= description of the vertical axis given as {lowest value} to {highest value} by {distance between major tick marks}.
 If you do not specify AXORDV, the macro can automatically specify one, but it may not be as good looking or intuitive as one you specify yourself.
 There should be 8-12 major tick marks.
 Giving too few makes the graph hard to read.
 Giving too many may result in values overwriting each other.
 OPTIONAL

VLABELSTYLE=V, Whether you want the label for the vertical axis to print parallel to the axis or horizontally (vlabelstyle=H, easier to read, but it usually takes up too much of the graphics area and squeezes the actual graph).
 OPTIONAL

HLABEL, The label for the horizontal axis.
 Be specific. Give a human-interpretable label with units, e.g. Weight (kg), not Weight, Years since randomization, not Time.
 NOTE: If there is punctuation (or a percent sign), you may need to use %str to keep the macro interpreter from misunderstanding the label
 OPTIONAL

AXORDH=, description of the horizontal axis.
 All remarks relating to AXORDV apply here too.
 OPTIONAL

PRINTLEGEND=T, Whether to print the legend for the graph.
 OPTIONAL

LEGLAB1=, LEGLAB2=,...LEGLAB10=, A set of (short) labels for the levels of BYVAR
 OPTIONAL

FONT=swiss A font for the graph.
 It is best to use a true-type font, rather than one that has to be simulated by your software
 OPTIONAL

TITLEMULT=1, A multiplier for the print of the graph title, if any.
 The interaction between fonts and output devices is complex, and this allows you to optimize the look of the title.
 OPTIONAL

AXLABMULT=1, A similar multiplier for the print of the axis labels.
 OPTIONAL

AXVALMULT=1, A similar multiplier for the print of the numeric values on the axis

OPTIONAL

CUTOFF=F, Whether to cut off the vertical axis at a specified value. Sometimes the upper confidence bound gets very high in areas of sparse data, to the extent that the prediction curve is squashed at the bottom of the graph, and its shape cannot be discerned. To make the confidence-cloud-making apparatus happy, the macro needs to know that values will not go higher than some level.

If a cutoff is used, it should be in the form

CUTOFF=2 x,

where x is a numeric value (e.g. 10).

OPTIONAL

BELOW ARE LINETYPES and COLORS for up to 10 lines (including confidence bounds).

=====

LINETYPE1 (solid line)=1,
LINETYPE2=20 (small dashed line),
LINETYPE3=35 (far apart dots),
LINETYPE4=4 (medium dashed line),
LINETYPE5=8 (dot and dashed line),
LINETYPE6=40 (2- and 3- groups of dots line),
LINETYPE7 (very long dashed line)=7,
LINETYPE8=2 (medium dashed and dot line),
LINETYPE9=30 (long, short, and medium patterns of dots line),
LINETYPE10=34 (dotted line), The types of lines used for the plot.

See SAS GRAPH documentation

(search sas graph line types and scroll to Specifying Line Types).

COLOR1=black,
COLOR2=red,
COLOR3=tan,
COLOR4=lib, (light blue)
COLOR5=gold,
COLOR6=violet,
COLOR7=pink,
COLOR8=ligr, (light gray)
COLOR9=libr, (light brown)
COLOR10=pagr, (pale gray) The colors for the lines used.

NOTE: Because of red-green color-blindness, we have not included any shades of green.

NOTE: The actual shades of pale gray and light gray vary by device used.

PRINTCV=F, Whether to print the variance-covariance matrix of the coefficients
OPTIONAL

PRINTPOINTS=, A space-delimited list of values for EXPOSURE for which you want to print out the estimates and 95% confidence limits.

You might use this for values you want to describe in the text of a paper or to put in a table.

OPTIONAL

NG=500, The number of points to make for plotting.

This works fine. no reason to change it.
OPTIONAL

PARAMETERS RELATING TO THE SMOOTHED HISTOGRAM

=====

The 2 parameters below relate to the level of smoothing.
If there are no problems making the graph, these should be left at their defaults.
BWM=1, The band width multiplier. Raising this makes the graph
more smoothe
OPTIONAL

DISTMETH=SJPI, The smoothing method for making the smoothed histogram.
Other options are OS and SROT.
OPTIONAL

PARAMETERS RELATING TO TEXT OUTPUT OF PLOTTING POINTS

=====

PLOTDATA=&EXPOSURE..&OUTCOME..SEL&SELECT._&NK,
The name of the file of plotting points.
We strongly suggest that you give this file a
mnemonic name to avoid overwriting.
On a UNIX system, this file will be in the same
directory as the program.
OPTIONAL

COMMTYPE=1,
OPTIONAL

FILEMODE=mod,
OPTIONAL

3 Examples

The first three examples are from the same study of BMI and ovulatory infertility used in the documentation for %LGTPHCURV9. Since this is a case-control study, we need to use the LOGIT link and plot the odds ratio. Also, since the unit of analysis is the pregnancy, and we do not want to use the empirical variance, even though some subjects may have more than one pregnancy included in the study, we have to 'fool' the macro into using ordinary PROC GENMOD by not telling it the *SUBJECT* variable name.

3.1 Example 1. A minimal call to the macro

```
title2 'example 1--bare bones';  
%glmcurv9(data=merge0, exposure=BMI, outcome=case,  
          dist=bin, link=logit, plotor=T,  
          reptype=ind,  
          adj= age2 age3 age4 period2 period3);
```

You get a WARNING from SAS,

WARNING: The variable SCALE in the DROP, KEEP, or RENAME list has never been

referenced.

You can safely ignore this.

The results are

```
/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03      1
example 1--bare bones
Percent of range of BMI below the first knot is 11 .
Percent of range of BMI above the last knot is 38 .
```

```
/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03      2
example 1--bare bones
  Knots for BMI:
  18.64 21.14 23.52 31.02
```

```
/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03      3
example 1--bare bones
```

values of spline variables when BMI is 16.07000000 and for extrapoints, if any

Obs	BMI	BMI1	BMI2
27103	16.07	0	0
27604	16.07	0	0

```
/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03      4
example 1--bare bones
27102 subjects with 27102 observations
model with adjusters only
```

Obs	VARNAME	DF	COEFF	STDERR	LOWERWALDCL	UPPERWALDCL	CHISQ	P
1	Intercept	1	-3.3729	0.0659	-3.5021	-3.2437	2618.30	<.0001
2	AGE2	1	-0.2041	0.0813	-0.3634	-0.0448	6.31	0.0120
3	AGE3	1	-0.2336	0.1075	-0.4443	-0.0230	4.73	0.0297
4	AGE4	1	0.5816	0.1774	0.2339	0.9293	10.75	0.0010
5	PERIOD2	1	0.1406	0.0798	-0.0159	0.2971	3.10	0.0782
6	PERIOD3	1	-0.0415	0.0988	-0.2353	0.1522	0.18	0.6744
7	Scale	0	1.0000	0.0000	1.0000	1.0000	-	-

/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03
 example 1--bare bones
 27102 subjects with 27102 observations
 model with linear exposure

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Obs	VARNAME	DF	COEFF	STDERR	LOWERWALDCL	UPPERWALDCL	CHISQ	P
1	Intercept	1	-4.6925	0.1989	-5.0823	-4.3026	556.59	<.0001
2	BMI	1	0.0573	0.0080	0.0416	0.0730	51.30	<.0001
3	AGE2	1	-0.2243	0.0814	-0.3839	-0.0648	7.59	0.0059
4	AGE3	1	-0.2798	0.1078	-0.4910	-0.0686	6.74	0.0094
5	AGE4	1	0.5219	0.1779	0.1732	0.8705	8.61	0.0034
6	PERIOD2	1	0.1280	0.0799	-0.0287	0.2847	2.56	0.1094
7	PERIOD3	1	-0.0780	0.0991	-0.2722	0.1162	0.62	0.4311
8	Scale	0	1.0000	0.0000	1.0000	1.0000	-	-

/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03
 example 1--bare bones
 27102 subjects with 27102 observations
 model with splines, if any

6

Obs	VARNAME	DF	COEFF	STDERR	LOWERWALDCL	UPPERWALDCL	CHISQ	P
1	Intercept	1	1.2414	1.0421	-0.8010	3.2839	1.42	0.2335
2	BMI	1	-0.2376	0.0527	-0.3410	-0.1343	20.31	<.0001
3	BMI1	1	1.4023	0.3517	0.7129	2.0916	15.89	<.0001
4	BMI2	1	-2.8876	0.8168	-4.4884	-1.2867	12.50	0.0004
5	AGE2	1	-0.2091	0.0816	-0.3690	-0.0492	6.57	0.0104
6	AGE3	1	-0.2545	0.1081	-0.4663	-0.0426	5.54	0.0185
7	AGE4	1	0.5610	0.1785	0.2111	0.9109	9.87	0.0017
8	PERIOD2	1	0.1342	0.0801	-0.0227	0.2911	2.81	0.0936
9	PERIOD3	1	-0.0748	0.0993	-0.2693	0.1198	0.57	0.4514
10	Scale	0	1.0000	0.0000	1.0000	1.0000	-	-

/udd/stleh/doctn/glmcurv Program example1-6 07OCT2014 18:03
 example 1--bare bones
 27102 subjects with 27102 observations

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Number of observations in the whole data set: 27102

Dependent variable: CASE

Exposure: BMI

Range of exposure in data used: 16.07 to 39.99

Number of knots: 4

You chose to use all 2 spline variables: BMI1 BMI2

Adjusted for:

AGE2 AGE3 AGE4 PERIOD2 PERIOD3

The DISTRIBUTION (DIST) is B and the LINK function is LOGIT

CASE and BMI

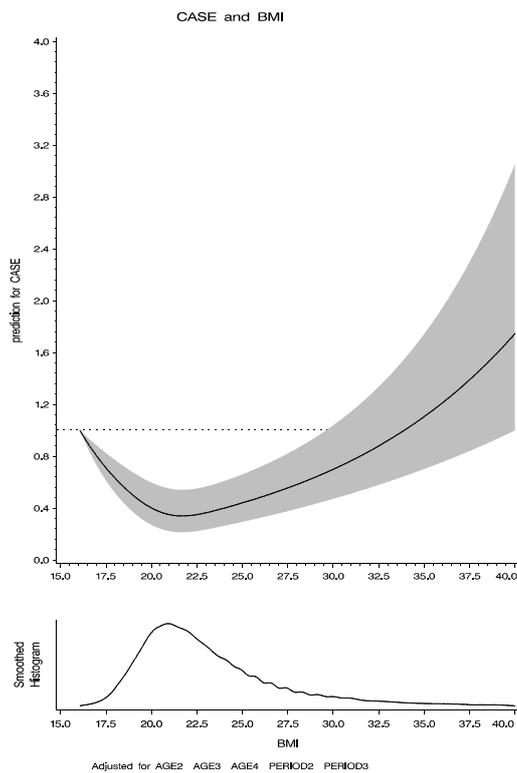
Name of graph file: MERGE0.BMI.CASE.sel1_4.PS

Graph option: SPLINE

Line Test Name	Description	P value
1	Test for curvature (i.e. non-linear relation)	If the P value is small, the relationship between the exposure and the outcome, if any, is non-linear. SEE LINE 2. If the P value is large, the relationship between the exposure and the outcome, if any is linear SEE LINE 3. Using likelihood ratio test, p-value is: <.0001
2	Test for overall significance of the curve	If LINE 1 indicated a possible non-linear relation between the exposure and the outcome, use this P value to express the the significance of the exposure-outcome Using likelihood ratio test, p-value is: <.0001
3	Test for linear relation	If the result of LINE 1 indicated no significant nonlinearity between the exposure and the outcome, use this P value AND rerun your model with the parameter PWHICH=LINEAR, to get the graph corresponding to the model of interest (if you intend to use the graph). Using likelihood ratio test, p-value is: <.0001

The output gives the graph name, which is the default.

The graph is



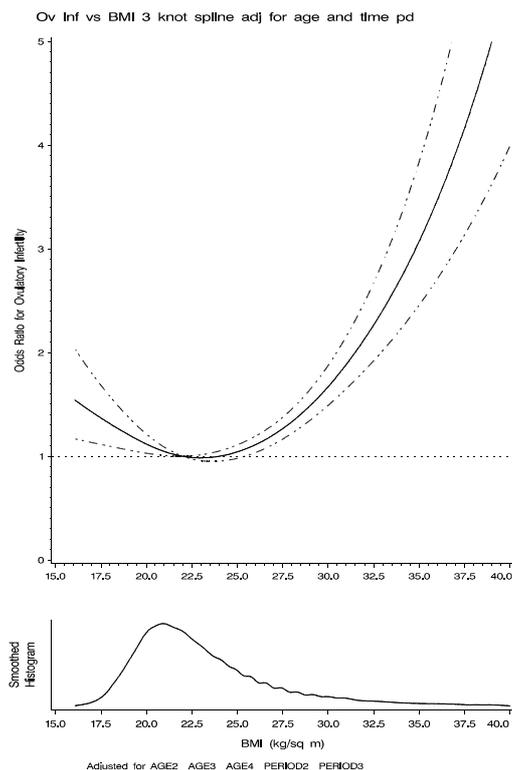
Since we did not give a reference value, the macro used the default, *MIN*.

3.2 Example 2. A more specified call with $NK=3$

Here we changed the reference value to 22. The macro call is

```
%glmcurv9(data=merge0, refval=22, exposure=BMI, outcome=case,
  retype=ind,
  dist=bin, link=logit, plotor=t,
  pictname=example2.ps, ci=F,
  axordv=0 to 5 by 1,
  hlabel=%quote(BMI (kg/sq m)), nk=3,
  vlabel=Odds Ratio for Ovulatory Infertility,
  adj= age2 age3 age4 period2 period3,
  graphtit=0v Inf vs BMI 3 knot spline adj for age and time pd,
  testrep=short,
  modprint=f);
```

and the graph is



The graph is (roughly) the same shape as in Example 1, but has moved up because we set $REFVAL=22$. Since CI is not equal to T , we got dotted lines for the confidence limits instead of a confidence cloud.

3.3 Example 3. Using 5-knot splines, `USERSPLV`, making a file of plotting points, and showing the use of `PRINTPOINTS`

In this and future examples we will use $TESTREP=SHORT$.
The macro call is

```

title2 'example 3--5 knot spline, given knots';
%glmcurv9(data=merge0, refval=22, exposure=BMI, outcome=case,
  retype=ind,
  link=logit, dist=bin,
  plotor=t,
  pictname=example3a.ps, outplot=ps,
  hlabel=%quote(BMI (kg/sq m)), knot=18.64 21.14 23.52 31.02 36.5,
  vlabel=Odds Ratio for Ovulatory Infertility,
  vlabelstyle=h,
  printpoints=18.5 21.75 25 27.5 30 32.5 35 37.5,
  axlabmult=1.5, axvalmult=1.1,
  adj= age2 age3 age4 period2 period3, select=1, plot=4,
  graphtit=Ov Inf vs BMI 5 knot spline adj for age and time pd,
  testrep=short,
  axordv=0 to 5 by .5);
data plotdat; infile '/udd/stleh/doctn/glmcurv/BMI.CASE.sel1_5' missover firstobs=2;
input mvarbl bmi estimate lower upper;

```

```
run;
title3 'first 5 observations of the plotting points file';
proc print data=plotdat (obs=5); run;
```

and the first 5 plotting points are

```
-----
/udd/stleh/doctn/glmcurv Program example1-6 01DEC2011 15:22          9
example 3--5 knot spline, given knots
first 5 observations of the plotting points file
```

Obs	MVARBL	BMI	ESTIMATE	LOWER	UPPER
1	1	16.0700	0.078232	.003016999	0.70417
2	1	16.1178	0.077514	.002970151	0.70328
3	1	16.1657	0.076802	.002924006	0.70238
4	1	16.2135	0.076096	.002878556	0.70148
5	1	16.2614	0.075396	.002833788	0.70058

The graphed values for the levels of BMI in *PRINTPOINTS* are

```
-----
/udd/stleh/doctn/glmcurv Program example1-6 01DEC2011 15:22          8
example 3--5 knot spline, given knots
20516 subjects with 27102 observations
Predicted values of CASE and 95% confidence bounds at designated values of BMI
for MVARBL = 1
```

Obs	BMI	predicted value	lower 95% confidence bound for predicted value	upper 95% confidence bound for predicted value
502	18.50	1.63251	1.30629	2.04018
503	21.75	1.00138	0.98549	1.01753
504	25.00	1.23759	1.04945	1.45946
505	27.50	1.64855	1.38231	1.96608
506	30.00	2.20710	1.78329	2.73162
507	32.50	2.76968	2.20173	3.48413
508	35.00	3.23774	2.55611	4.10113
509	37.50	3.68193	2.62679	5.16092
510	22.00	1.00000	1.00000	1.00000

3.4 Example 4. An example with multiple observations per subject

This example comes from the Trial of Vitamins in HIV-positive pregnant women in Tanzania. We look at the relation of CD4 count (a measure of immune function) and age in their children. The macro call is

```
%glmcurv9(data=cd4kid, subject=idno2, outcome=cd4c, exposure=agemon,
  distmeth=os, displayx=t, bwm=5,
  select=3, dist=n, link=id,
  knot=0 6 12 24 36 48,
  pictname=cd4.glmselect.6kn.ps,
  testrep=short,
  maxstep=2,
  plotor=f);
```

Since we had trouble with the smoothed histogram when we used the default options, we switched to *DISTMETH=OS*. The output is

```
-----
The SAS System                                13:55 Tuesday, October 7, 2014    1
Percent of range of AGEMON below first knot is 0  .
Percent of range of AGEMON above last knot is 19  .
```

```
-----
The SAS System                                13:55 Tuesday, October 7, 2014    2
  Knots for AGEMON:
  0 6 12 24 36 48
```

```
-----
The SAS System                                13:55 Tuesday, October 7, 2014    3
```

values of spline variables when AGEMON is 0.00000000 and for extrapoints, if a

Obs	AGEMON	AGEMON1	AGEMON2	AGEMON3	AGEMON4
3571	0	0	0	0	0
4072	0	0	0	0	0

```
-----
The SAS System                                13:55 Tuesday, October 7, 2014    4
```

809 subjects with 3570 observations
model with adjusters only

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1533.097	18.8536	1496.145	1570.050	81.32	<.0001

The SAS System 13:55 Tuesday, October 7, 2014 5

809 subjects with 3570 observations
model with linear exposure

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1543.759	19.8856	1504.784	1582.734	77.63	<.0001
2	AGEMON	-0.7977	0.9148	-2.5906	0.9952	-0.87	0.3832

The SAS System 13:55 Tuesday, October 7, 2014 6

809 subjects with 3570 observations
automatic gee selection
Step 0 : variable AGEMON1 added

The SAS System 13:55 Tuesday, October 7, 2014 7

809 subjects with 3570 observations
automatic gee selection
Step 1 : No variable dropped.

The SAS System 13:55 Tuesday, October 7, 2014 8

809 subjects with 3570 observations
automatic gee selection
Step 2 : variable AGEMON2 added

The SAS System 13:55 Tuesday, October 7, 2014 9

809 subjects with 3570 observations
automatic gee selection
Step 3 : No variable dropped.

The SAS System 13:55 Tuesday, October 7, 2014 10

809 subjects with 3570 observations
automatic gee selection
Step 4 : variable AGEMON3 added

The SAS System 13:55 Tuesday, October 7, 2014 11

809 subjects with 3570 observations
automatic gee selection
Step 5 : No variable dropped.

The SAS System 13:55 Tuesday, October 7, 2014 12

809 subjects with 3570 observations
automatic gee selection
Step 6 : no variable added

The SAS System 13:55 Tuesday, October 7, 2014 13

809 subjects with 3570 observations
automatic gee selection
Step 7 : No variable dropped.

The SAS System 13:55 Tuesday, October 7, 2014 14

809 subjects with 3570 observations
model with splines, if any

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1318.023	26.1281	1266.813	1369.234	50.44	<.0001
2	AGEMON	76.3522	7.7337	61.1944	91.5099	9.87	<.0001
3	AGEMON1	-1012.46	125.7902	-1259.00	-765.915	-8.05	<.0001
4	AGEMON2	2120.408	286.3144	1559.242	2681.574	7.41	<.0001
5	AGEMON3	-1148.09	176.2403	-1493.51	-802.662	-6.51	<.0001

The SAS System 13:55 Tuesday, October 7, 2014 15

809 subjects with 3570 observations

Number of observations in the whole data set: 3570

Dependent variable: CD4C

Exposure: AGEMON

Range of exposure in data used: 0 to 59.539473684

Number of knots: 6

Spline variable(s) selected by stepwise: AGEMON1 AGEMON2 AGEMON3

Not adjusted

The DISTRIBUTION (DIST) is N and the LINK function is ID

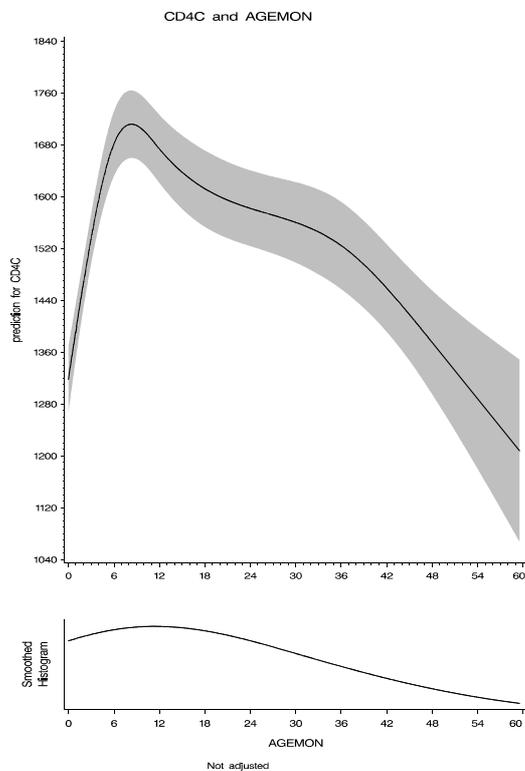
CD4C and AGEMON

Name of graph file: cd4.glmselect.6kn.ps

Graph option: SPLINE

Line Test Name	P value
1 Test for curvature (i.e. non-linear relation)	<.0001
2 Test for overall significance of curve	<.0001
3 Test for linear relation	0.3866

The graph is



3.5 Example 5. An example with multiple observations per person and MDEP(1) working covariance structure

This example and the next are from the trial of vitamins in HIV-negative pregnant women in Tanzania. It investigates whether the relationship between energy intake (ascertained from 24 hour recalls) and weight gain (in grams per 4 weeks) is nonlinear.

The covariate `difftimec4` is the number of weeks between the measurements -4 (since the average time between visits was 4 weeks).

The first time we ran the macro with `nk=4`, 34% of the range of the exposure was above the highest knot. We therefore added a knot at 3600.

```
%glmcurv9(data=final, subject=idno2, reptype=mdep(1), outcome=diffwt,
dist=n, link=id,
refval=2200,
knot=1185 1899 2344 3056 3600,
pictname=wtgainpreg.energy.ps,
axordv=600 to 1800 by 100,
vlabel=%str(Predicted 4-week weight gain during pregnancy (grams) ),
axordh=0 to 5000 by 500, hlabel=%str(Energy intake (kcal) ),
testrep=short,
cutoff=2 1800,
exposure=energy, adj=difftimec4, adjdat=adjdat);
```

The output is

```
-----
/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 2
Percent of range of ENERGY below first knot is 18 .
Percent of range of ENERGY above last knot is 20 .
```

```
-----
/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 3
Knots for ENERGY:
1185 1899 2344 3056 3600
```

```
-----
/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 4
```

values of spline variables when ENERGY is 2200 and for extrapolants, if any

Obs	ENERGY	ENERGY1	ENERGY2	ENERGY3
14564	2200	179.293	4.67590	0

/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 5

6761 subjects with 14062 observations
model with adjusters only

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1360.842	12.5110	1336.321	1385.363	108.77	<.0001
2	DIFFTIMEC4	245.4710	46.1888	154.9426	335.9994	5.31	<.0001

/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 6

6761 subjects with 14062 observations
model with linear exposure

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1105.471	48.3168	1010.771	1200.170	22.88	<.0001
2	ENERGY	0.1203	0.0220	0.0772	0.1635	5.47	<.0001
3	DIFFTIMEC4	242.8707	46.1560	152.4066	333.3349	5.26	<.0001

/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 7

6761 subjects with 14062 observations
model with splines, if any

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1073.936	125.9471	827.0843	1320.788	8.53	<.0001
2	ENERGY	0.1255	0.0856	-0.0423	0.2933	1.47	0.1426
3	ENERGY1	0.4241	0.4476	-0.4532	1.3013	0.95	0.3434
4	ENERGY2	-3.4259	2.1475	-7.6349	0.7831	-1.60	0.1106
5	ENERGY3	5.9696	3.0865	-0.0798	12.0191	1.93	0.0531
6	DIFFTIMEC4	241.3327	46.1554	150.8698	331.7955	5.23	<.0001

/udd/stleh/doctn/glmcurv Program paper1 12JUN2012 13:45 stleh 8

6761 subjects with 14062 observations

Number of observations in the whole data set: 14062

Dependent variable: DIFFWT

Exposure: ENERGY

Range of exposure in data used: 502.4 to 4357.65

Number of knots: 5

You chose to use all 3 spline variables: ENERGY1 ENERGY2 ENERGY3

Adjusted for:

DIFFTIMEC4

The DISTRIBUTION (DIST) is N and the LINK function is ID

DIFFWT and ENERGY

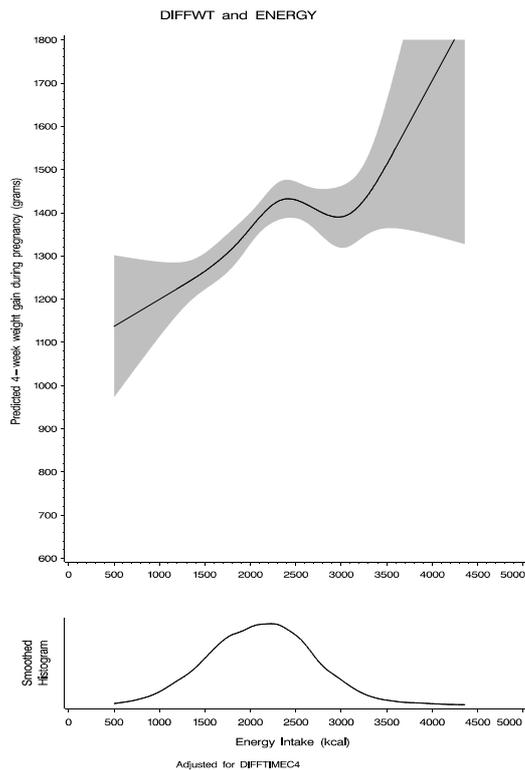
Name of graph file: wtgainpreg.energy.ps

Graph option: SPLINE

Line Test Name	P value
1 Test for curvature (i.e. non-linear relation)	0.0712
2 Test for overall significance of curve	<.0001
3 Test for linear relation	<.0001

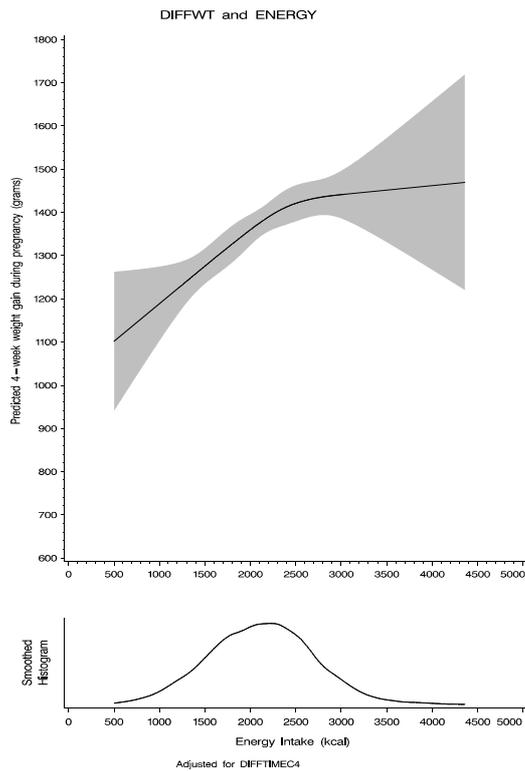
Note that we did not use automatic selection.

The graph is



Since the test for nonlinearity is not significant, we would be unlikely to include this graph in a paper.

For comparison, we show the graph obtained from a call to the macro using the default 4 knots.



The LINE 1 p-value for this analysis was .25.

3.6 Example 6. Using BYVAR, AXLABMULT, and other customizations, as well as automatic selection without specifying the number of knots

As an example, we will stratify the dataset used in Example 5 by BMI at entry to the study. The macro call is

```
%glmcurv9(data=final, subject=idno2, reptype=mdep(1), outcome=diffwt,
dist=n,
select=3,
refval=2000,
printpoints=1500 1800 2000 2200 2500,
byvar=bmi1825,
where=bmi1825 ne .,
shortlegend=t,
leglab1=BMI ge 25, leglab2=BMI lt 25,
graphtit=Monthly weight gain in pregnancy by Energy intake and BMI,
footer=Adjusted for length of time interval,
pictname=wtgainpreg.enbmib.ps,
axordv=600 to 1800 by 100,
vlabel=%str(Predicted 4-week weight gain during pregnancy (grams) ),
axordh=0 to 5000 by 500,
hlabel=%str(Energy intake (kcal) ),
axlabmult=1.5,
testrep=short,
cutoff=2 1800,
```

exposure=energy, adj=difftimec4 , adjdat=adjdat1);

The output is

```
-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 2
WARNING in macro call: since no link is provided,
      the default canonical link function for N , ID , will be used.
```

```
-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 3
Percent of range of ENERGY below the first knot is 9 .
Percent of range of ENERGY above the last knot is 22 .
```

```
-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 4
Knots for ENERGY:
839.91667 1131.65 1354.28 1508.183 1626.15417 1724.1625 1808.9324 1892.28
1977.0625 2050.9125 2126.5575 2202.06875 2272.875 2343.65813 2418.20833 2499.7
625
2581.4975 2682.55 2823.93333 3010.52625 3520.9225
```

```
-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 5
```

values of spline variables when ENERGY is 2000 and for extrapoints, if any

	E	E	E	E	E	E	E	E	E
	N	N	N	N	N	N	N	N	N
	E	E	E	E	E	E	E	E	E
	R	R	R	R	R	R	R	R	R
0	R	G	G	G	G	G	G	G	G
b	G	Y	Y	Y	Y	Y	Y	Y	Y
s	Y	1	2	3	4	5	6	7	8
12726	1500	40.013	6.953	0.430	0.000	0.0000	0.0000	0.0000	0.0000
12727	1800	123.121	41.535	12.319	3.457	0.7310	0.0607	0.0000	0.0000
12728	2000	217.206	91.094	37.457	16.551	7.2691	2.9199	0.9704	0.1739
12729	2200	350.027	169.647	84.156	46.066	26.2900	14.9893	8.3207	4.0539
12730	2500	636.494	356.448	209.238	135.737	92.8344	64.9706	45.9162	31.2259
12731	2000	217.206	91.094	37.457	16.551	7.2691	2.9199	0.9704	0.1739

	E	E	E	E	E	E	E	E	E E E
E	N	N	N	N	N	N	N	N	N N N
N	E	E	E	E	E	E	E	E	E E E
E	R	R	R	R	R	R	R	R	R R R
R	G	G	G	G	G	G	G	G	G G G
O	G	Y	Y	Y	Y	Y	Y	Y	Y Y Y
b	Y	1	1	1	1	1	1	1	1 1 1
s	9	0	1	2	3	4	5	6	7 8 9

12726	0.0000	0.0000	0.00000	0.00000	0.00000	0.00000	0.000000		0 0 0 0
12727	0.0000	0.0000	0.00000	0.00000	0.00000	0.00000	0.000000		0 0 0 0
12728	0.0017	0.0000	0.00000	0.00000	0.00000	0.00000	0.000000		0 0 0 0
12729	1.5415	0.4610	0.05511	0.00000	0.00000	0.00000	0.000000		0 0 0 0
12730	19.8955	12.6008	7.24562	3.67919	1.63004	0.53166	0.076126	1.8638E-9	0 0 0 0
12731	0.0017	0.0000	0.00000	0.00000	0.00000	0.00000	0.000000		0 0 0 0

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 6
 For the stratum bmi1825=0 (BMI ge 25)
 2298 subjects with 4675 observations
 model with adjusters only

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1254.305	23.0996	1209.030	1299.579	54.30	<.0001
2	DIFFTIMEC4	294.0854	84.3627	128.7375	459.4332	3.49	0.0005

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 7
 For the stratum bmi1825=0 (BMI ge 25)
 2298 subjects with 4675 observations
 model with linear exposure

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	951.8493	85.6149	784.0472	1119.651	11.12	<.0001
2	ENERGY	0.1436	0.0398	0.0657	0.2216	3.61	0.0003
3	DIFFTIMEC4	288.7176	84.5548	122.9931	454.4420	3.41	0.0006

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 8
 For the stratum bmi1825=0 (BMI ge 25)
 2298 subjects with 4675 observations
 automatic gee selection
 Step 0 : no variable added

```

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 9
For the stratum bmi1825=0 (BMI ge 25)
2298 subjects with 4675 observations
automatic gee selection
stepwise procedure cannot add or drop more variables.

```

```

-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 10
For the stratum bmi1825=0 (BMI ge 25)
2298 subjects with 4675 observations
  No spline variables are selected by the current criteria.
  You can either change the parameter values for sls, sle or nk, or
  bear in mind that the only valid test is the linear test.
  The graph output will be the linear graph.

```

```

-----
/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 11
For the stratum bmi1825=0 (BMI ge 25)
2298 subjects with 4675 observations
  Number of observations in the whole data set: 12224
  number of observations in the stratum BMI1825=1: .

```

```

  Dependent variable: DIFFWT
  Exposure: ENERGY
  Range of exposure in data used: 502.4 to 4357.65
  Number of knots: 21
  No spline variable selected by the current criteria
  Adjusted for:
    DIFFTIMEC4

```

The DISTRIBUTION (DIST) is N and the LINK function is ID

```

  Monthly weight gain in pregnancy by Energy intake and BMI
  Name of graph file: wtgainpreg.enbmib.ps
  Graph option: LINEAR

```

No spline variables were selected. There is no spline model.
The p-values for lines 1 and 2 will therefore be missing.

Line	Test Name	P value
1	Test for curvature (i.e. non-linear relation)	.
2	Test for overall significance of curve	.
3	Test for linear relation	0.0003

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 12
 For the stratum bmi1825=0 (BMI ge 25)
 2298 subjects with 4675 observations
 Predicted values of DIFFWT and 95% confidence bounds at designated values of E
 for bmi1825 = 0

Obs	ENERGY	predicted value	lower 95% confidence bound for predicted value	upper 95% confidence bound for predicted value
502	1500	1167.28	1103.76	1230.80
503	1800	1210.36	1160.46	1260.26
504	2000	1239.09	1193.61	1284.56
505	2200	1267.81	1221.64	1313.98
506	2500	1310.90	1254.88	1366.91
507	2000	1239.09	1193.61	1284.56

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 13
 For the stratum bmi1825=1 (BMI lt 25)
 3618 subjects with 7549 observations
 model with adjusters only

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1430.817	16.1385	1399.186	1462.448	88.66	<.0001
2	DIFFTIMEC4	258.7568	59.9751	141.2078	376.3058	4.31	<.0001

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 14
 For the stratum bmi1825=1 (BMI lt 25)
 3618 subjects with 7549 observations
 model with linear exposure

Obs	VARNAME	COEFF	STDERR	LOWERCL	UPPERCL	Z	P
1	Intercept	1292.287	63.2840	1168.252	1416.321	20.42	<.0001
2	ENERGY	0.0645	0.0285	0.0085	0.1204	2.26	0.0239
3	DIFFTIMEC4	258.1707	59.9108	140.7477	375.5937	4.31	<.0001

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 15
 For the stratum bmi1825=1 (BMI lt 25)

3618 subjects with 7549 observations
automatic gee selection
Step 0 : no variable added

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 16
For the stratum bmi1825=1 (BMI lt 25)
3618 subjects with 7549 observations
automatic gee selection
stepwise procedure cannot add or drop more variables.

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 17
For the stratum bmi1825=1 (BMI lt 25)
3618 subjects with 7549 observations
No spline variables are selected by the current criteria.
You can either change the parameter values for sls, sle or nk, or
bear in mind that the only valid test is the linear test.
The graph output will be the linear graph.

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 18
For the stratum bmi1825=1 (BMI lt 25)
3618 subjects with 7549 observations
Number of observations in the whole data set: 12224
number of observations in the stratum BMI1825=2: .

Dependent variable: DIFFWT
Exposure: ENERGY
Range of exposure in data used: 502.4 to 4357.65
Number of knots: 21
No spline variable selected by the current criteria
Adjusted for:
DIFFTIMEC4

The DISTRIBUTION (DIST) is N and the LINK function is ID

Monthly weight gain in pregnancy by Energy intake and BMI
Name of graph file: wtgainpreg.enbmib.ps
Graph option: LINEAR

No spline variables were selected. There is no spline model.
The p-values for lines 1 and 2 will therefore be missing.

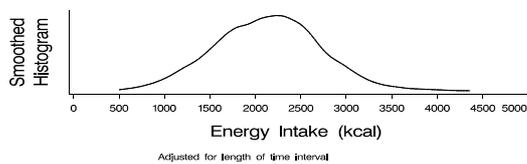
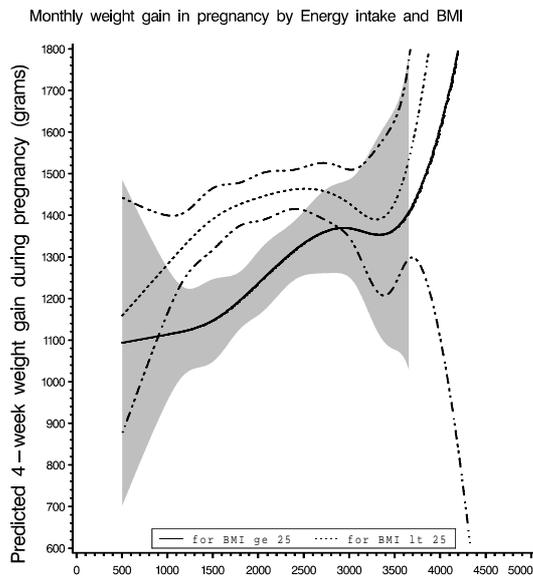
Line Test Name	P value
----------------	---------

- 1 Test for curvature (i.e. non-linear relation) .
- 2 Test for overall significance of curve .
- 3 Test for linear relation 0.0243

/udd/stleh/doctn/glmcurv Program paper1 07OCT2014 18:02 stleh 19
 For the stratum bmi1825=1 (BMI lt 25)
 3618 subjects with 7549 observations
 Predicted values of DIFFWT and 95% confidence bounds at designated values of E
 for bmi1825 = 1

Obs	ENERGY	predicted value	lower 95% confidence bound for predicted value	upper 95% confidence bound for predicted value
502	1500	1388.98	1341.03	1436.94
503	1800	1408.32	1371.29	1445.35
504	2000	1421.22	1388.58	1453.85
505	2200	1434.11	1402.34	1465.88
506	2500	1453.45	1416.10	1490.80
507	2000	1421.22	1388.58	1453.85

The graph is



Since the macro did not select any spline variables in either stratum of BMI, it plotted the linear relationships.

4 Computational Methods

4.1 Automatic knot placement, given a desired number of knot points

If you specify a number of knots (NK), the macro will automatically determine the appropriate percentiles of the data and place the knots there. If you request automatic spline variable selection ($SELECT=3$) and have not given NK , the macro will set $NK=21$. If you do not give NK or $KNOT$ and do not use automatic spline variable selection, the macro will set $NK=4$. As always, this can be overridden by providing a list of knot locations.

```
NK  Knot locations as percentiles of EXPOSURE
--  -----
3   5 50 95
4   5 35 65 95
5   5 27.5 50 72.5 95
6   5 23 41 59 77 95
7   2.5 18.3333 34.1667 50 65.8333 81.6667 97.5
8   1 15 29 43 57 71 85 99
9   2 14 26 38 50 62 74 86 98
10  2 12.6667 23.3333 34 44.6667 55.3333 66
    76.6667 87.3333 98
17  2 8 14 20 26 32 38 44 50 56 62 68 74 80 86 92 98
21  1 4 9 14 19 24 29 34 39 44 49 54 59 64 69 74 79 84 89 94 99
25  2 6 10 14 18 22 26 30 34 38 42 46 50
    54 58 62 66 70 74 78 82 86 90 94 98
50  1 3 5 7 9 11 13 15 17 19 21 23 25 27
    29 31 33 35 37 39 41 43 45 47 49 51
    53 55 57 59 61 63 65 67 69 71 73 75
    77 79 81 83 85 87 89 91 93 95 97 99
```

4.2 Computation of the spline variables:

Let t_j be the j th knot point.

Let $kd = (t_{nk} - t_1)^{2/3}$, where kd is a normalizing parameter to get the spline variables back into the original units.

For a level of the exposure x , x_j , the value of the j th spline variable (j runs from 1 to $NK-2$) is given by

$$x_j = \max((x - t_j)/kd, 0)^3 + (t_{nk-1} - t_j) * \max((x - t_{nk})/kd, 0)^3 - (t_{nk} - t_j) * \max((x - t_{nk-1})/kd, 0)^3 / (t_{nk} - t_{nk-1})$$

For $x < t_j$ the value of the j th spline variable is 0 (as are the 'higher' spline variables) (because all the 'max' values are 0, since $x < t_j < t_{nk-1} < t_{nk}$. As x gets larger, it has more and more nonzero spline variables.

Note that the value of x_j depends on the values of the first, nk th, and $nk-1$ st knots. That is why the value of the spline variable depends on the locations of knots other than the j th knot.

4.3 Default bandwidth for smoothing:

The default bandwidth is data-specific. Let N be the size of the data set, and STD be the standard deviation of the exposure variable (X) in the data set.

$$bandwidth = (STD/1.349) * (4/3N)^{0.2}$$

Although the user can set the bandwidth (using BWM), it is usually fine to let the macro do it automatically. See Frequently Asked Questions below.

4.4 Outline of stepwise model selection:

If you request automatic spline variable selection (em $SELECT=3$) and have not specified NK , the macro will set $NK=21$. As always, this can be overridden by providing a list of knot locations.

The default SLE and SLS for automatic selection are .05, but the user may specify other values.

In the discussion below, all mentions of 'likelihood' should be interpreted to mean 'partial likelihood' when Cox models are used.

Each step starts with a 'base' model. For the first step, the 'base' model includes the linear term and all the adjusters. For subsequent steps, the 'base' model includes the above plus whatever spline variables are in the model by the end of the step.

For a forward step, each of the spline variables not in the base model is added (singly) to the base model and a likelihood is computed. If, for the spline variable giving the biggest likelihood (i.e. the biggest change from the base model), the likelihood ratio test (LRT) gives a p-value meeting the criterion for entry into the model (SLE), that spline variable is added to the model. Otherwise, no variable is added to the model.

For a backward step, each of the spline variables in the base model is deleted (singly) from the base model, and a likelihood is computed. If, for the spline variable giving the biggest likelihood (i.e. the closest to the base model), the LRT gives a p-value greater than the criterion for staying in the model (SLS), that spline variable is dropped from the model. Otherwise, no variable is dropped. If a variable is dropped, the macro uses this new base model and tests the remaining spline variables to see whether they can be dropped.

Forward and backward steps alternate until two (2) steps in a row do not change the model, or until the maximum number of steps is attained (default=10).

5 Including the graph in a MS-WORD document

Below are the steps for importing an encapsulated postscript file into a MS-WORD document.

0. If you have a postscript graph, you may have to change the graph file's extension to 'eps' on the unix system.

1. E-mail the file to yourself as an attachment, and download to your PC.
2. Open your WORD document.
3. The sequence of keys (at least in Windows XP and its version of WORD) is


```
insert
picture
from file
<locate file>
convert file (this is a window that WORD gives you)
encapsulated postscript
```

NOTE: Conversion from encapsulated postscript may not be installed on your computer, but it is available for Windows 95 and beyond. NOTE: When I did the above procedure the picture on my Windows screen was fuzzy. When printed, it was crisp.

If you are really having trouble, consider using one of the other formats (HTML, JPEG, CGM).

6 How should I describe this in my Methods section?

The wording below has been approved by Prof. Donna Spiegelman.

We examined the possibly non-linear relation between *insert the name of the exposure here* and *insert the name of the outcome here, such as the RR of* — non-parametrically with restricted cubic splines [REF Durrleman and Simon]. Tests for non-linearity used the likelihood ratio test, comparing the model with only the linear term to the model with the linear and the cubic spline terms.

7 WARNINGS

Log-binomial models do not always converge, especially if they have many covariates or continuous variables. You may have to use the Poisson variance (Spiegelman and Hertzmark, AJE).

PROC GENMOD does not like missing values for *SUBJECT*, *WITHINVAR*. If you want to use observations with missing values for these variables, you need to use a 'fake' value for them.

If you are using a weighted model, observations with missing values for the weight variable will be deleted from the analysis.

8 Frequently Asked Questions

8.1 Q: Why does a variable named MVARBL keep showing up in my output?

A: , included for the convenience of the programmer MVARBL is the default value of *BYVAR*. It is 1 for all observations in the dataset.

8.2 Q: If the p-value for nonlinearity is greater than .05 but the p-value for the overall significance of the curve is less than .05, why can't I say that the relationship is nonlinear?

A: The overall significance of the curve is coming entirely from the linear relationship (line 3).

8.3 Q: Why does the confidence cloud stop abruptly in the middle of the graph?

A: This happens when the upper (or lower) confidence limit is out of the range of the vertical axis. To solve this for the lower bound, change the lower value in *AXORDV*. To solve this for the upper bound, you may change the upper bound or use the *CUTOFF* parameter.

8.4 Q: Why is the confidence band so wide?

A: A common reason for this is that parts of the range of the exposure have very few observations. This is most likely to occur at the extremes of the data. It shows up as long flat tails in the smoothed histogram. You can also look at the knot positions. For 3 and 4 knot splines, the outer knots are at the 5th and 95th percentile points. If these are far from the lowest and highest values in the data you are using, you may need to trim the data, either by values of the exposure (*HICUT*, *LOWCUT*) or by percentiles of the exposure distribution (*HPCT*, *LPCT*). If you cannot do that, then use the cutoff parameter.

8.5 Q: Why are the values on the horizontal axis printing out vertically?

A: You probably asked for too many major tick marks. *AXORDH* should be written so that about 8 to 12 numbers will print out, such as

```
axordh=0 to 100 by 10
```

rather than

```
axordh=0 to 100 by 5
```

This could also happen if you let the macro determine the tick marks and they are not 'round.' In this case, you should see what the graph looks like and determine the horizontal axis ticking yourself.

8.6 Q: I want to plot the smoothed histogram, but the SAS .log says that the Sheather-Jones plug-in did not converge

A: Sometimes the Sheather-Jones plug-in does not work. You can try increasing the smoothing parameter (*BWM*) or using *DISTMETH=OS*.

8.7 Q: Why are the coefficients of the spline variables so large in absolute value?

A: Because the spline variables are often highly correlated, it is not unusual for the coefficients to alternate between very negative and very positive values.

8.8 Q: I got an error saying the x-origin did not leave enough space for the text.

Here is an example of the ERROR message:

```
ERROR: The specified x-origin for the left vertical axis labeled LOWER did not
       leave enough space for the text. You need to specify ORIGIN=( 2.1 INCH
       ). The graph was not produced.
```

A: This can happen when you use *VLABELSTYLE=H*, if some of the words are too long. Try hyphenating the longest words OR change the *HORIGIN* as suggested by the ERROR message. This latter will make your actual graphics area smaller to accommodate your axis label.

8.9 Q: How do I make ADJDAT?

A: If you are plotting probabilities or incidence rates, you need to have values of the covariates at which to plot them. The choice of covariate values will influence the absolute value of the probabilities or incidence rates, but not the shape of the curve. It is often convenient to use the reference levels of all the sets of indicators (or alternatively, the middle indicator), and the medians or some conventional value for the continuous variables (other than the exposure, which should not have a value in this dataset). One way to do this, especially if you have a lot of sets of indicators is as follows:

```
data adjdat;
array nums ..... ; /* the list of all the adjusters. you can just copy it from the ADJ p
do over nums; nums=0; end ; /* effectively sets all sets of indicators to their referen
/* special coding for continuous variables */
bmi76=25; /* coding to a conventional cutoff */
run;
```

9 References

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Spiegelman, D, Hertzmark, E: The authors reply to Neogi & Zhang, Tian & Liu, and Petersen & Deddens re: 'Easy SAS calculations for risk or prevalence ratios and differences'. AJE 163(12): 1159-1161, 2006.

10 Credits

Written by Ellen Hertzmark, Ruifeng Li, Biling Hong, and Donna Spiegelman for the Channing Laboratory. Questions can be directed to Biling Hong, stbho@channing.harvard.edu, (617) 432-7336.