Genetics Studies of Comorbidity

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Outline

- Background
 - Comorbidity
 - Disorders, Genes and Covariates
- Weighted Association Test
 - Generalized Kendall's Tau
 - Asymptotic Distribution and Power
 - Application to WTCCC Bipolar Disorder Data
- Maximum Weighted Association Test
 - Asymptotic Distribution
 - Simulations
- Analysis of Comorbidity
 - Application to COGA Family Data
 - Application to SAGE GWAS Data
- Conclusions



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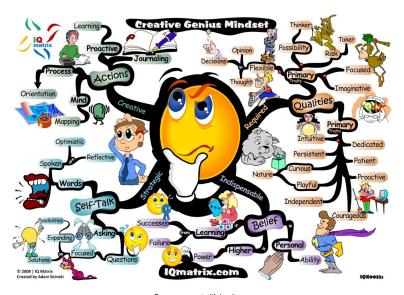
Comorbidity

Multiple disorders or illnesses occur in the same person, simultaneously or sequentially



Source: www.depressioncell.com; www.depressiondodging.com

Comorbidity



Source: aasets.lifehack.org

Comorbidity

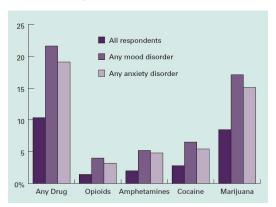


Dr. Volkow, Director, NIDA: Comorbidity is a topic that our stakeholders—patients, family members, health care professionals, and others—frequently ask about. It is also a topic about which we have insufficient information, so it remains a research priority for NIDA.

Source: www.nida.nih.gov

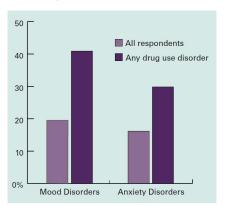
Possible Mechanisms for Comorbidity

- Mental disorder ⇒ drug use disorder
- Drug use disorder ⇒ mental disorder
- Common etiology \Rightarrow $\begin{cases} \text{mental disorder} \\ \text{drug use disorde} \end{cases}$



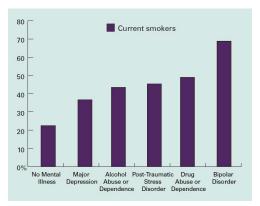
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Possible Mechanisms for Comorbidity

- Mental disorder ⇒ drug use disorder
 - Drug use disorder ⇒ mental disorder
- $\bullet \ \, \text{Common etiology} \Rightarrow \left\{ \begin{array}{l} \text{mental disorder} \\ \text{drug use disorder} \end{array} \right.$

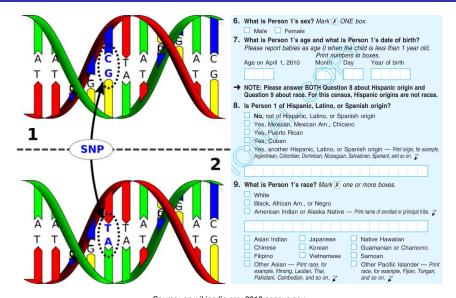


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Genotypes and Covariates



Source: en.wikipedia.org: 2010.census.gov

Disorders, Genes and Covariates



- Covariates: interact or confound genetic effects
- Failure to account for covariates: bias or reduced power

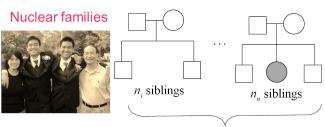
Study Design

Population-based studies





Family-based studies



n families

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Notation and Hypothesis

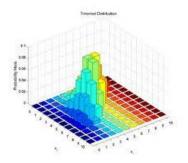
- n study subjects, from a population-based study or family-based study
- For each subject:
 - A vector of traits $\mathbf{T} = (T^{(1)}, \dots, T^{(p)})'$
 - Marker genotype M
 - Parental marker genotypes M^{pa} (only available in a family-based study)
 - A vector of covariates $\mathbf{Z} = (Z^{(1)}, \dots, Z^{(l)})'$
- Null hypothesis: no association between marker alleles and any linked locus that influences traits T

Typical Response

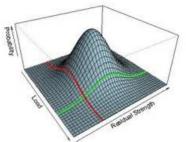
Fagerstrom Test for Nicotine Dependence

Quantitative Scale 1. (How many) cigarettes a day do you usually smoke? 1 to 10 0 point 21 to 30 2 points 11 to 20 1 point 30 or more 3 points **Ordinal Scale** 2. How soon after you wake up do you smoke your first cigarette? After 60 minutes 0 point 6 - 30 minutes 2 points 31-60 minutes < 5 minutes 1 point 3 points 3. Do you smoke more during the first two hours of the day than during the rest of the day? No 0 point Yes 1 point 4. Which cigarette would you most hate to give up? Any other cigarette than the first 0 point The first cigarette in the 1 point one morning 5. Do you find it difficult to refrain from smoking in places where it is forbidden, such as public buildings, on airplanes or at work? Dichotomous Scale Opoint 1 point 6. Do you still smoke even when you are so ill that you are in bed most of the day? No 0 point Yes 1 point

Multivariate Distributions



$$\prod_{t} \frac{n_{t}!}{\prod_{a} n_{t,a}!} \prod_{a} \hat{p}_{t,a}^{n_{t,a}}$$



$$\frac{\exp{\{-\frac{1}{2}(x-\mu)'\Sigma^{-1}(x-\mu)\}}}{\sqrt{(2\pi)^n|\Sigma|}}$$

Kendall's Tau

- A nonparametric statistic measuring the rank correlation between two variables
- Pairs of observations: $\{(X_i, Y_i) : i = 1, \dots, n\}$
- \bullet (X_i, Y_i) and (X_i, Y_i) :
 - Concordant, if $X_i X_i$ and $Y_i Y_i$ have the same sign
 - Disconcordant, if $X_i X_i$ and $Y_i Y_i$ have the different sign
- Kendall's tau:

$$\tau = 2(A - B) / \{n(n - 1)\}$$

A and B: numbers of concordant and disconcordant pairs

Or

$$\tau = \binom{n}{2}^{-1} \sum_{i < j} \operatorname{sign}\{(X_i - X_j)(Y_i - Y_j)\}$$



Generalized Kendall's Tau

- $\mathbf{F}_{ij} = \{f_1(T_i^{(1)} T_j^{(1)}), \dots, f_p(T_i^{(p)} T_j^{(p)})\}'$
 - $f_k(\cdot)$: identity function for a quantitative or binary trait
 - $f_k(\cdot)$: sign function for an ordinal trait
- $D_{ij} = C_i C_j$. C: number of any chosen allele in marker genotype M
- Genaralized Kendall's tau (Zhang, Liu and Wang, 2010):

$$\mathbf{U} = \binom{n}{2}^{-1} \sum_{i < j} D_{ij} \mathbf{F}_{ij}$$

- Special cases:
 - FBAT-GEE (Lange et al. 2003)
 - Test for a single ordinal trait (Wang, Ye and Zhang, 2006)

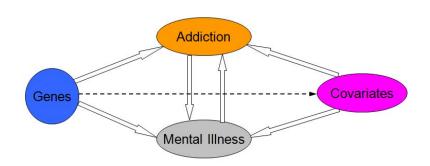


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Hypothesis with Covariates



 New null hypothesis: no association between marker alleles and any linked locus that influences traits T conditional on covariates Z

Weighted Test

- A weight function $w(\mathbf{Z}_i, \mathbf{Z}_i)$ imposes a relatively large weight when \mathbf{Z}_i is close to \mathbf{Z}_i , and a relatively small weight when \mathbf{Z}_i and \mathbf{Z}_i are far away
- Weighted U-statistic:

$$\mathbf{S} = \binom{n}{2}^{-1} \sum_{i < j} D_{ij} \mathbf{F}_{ij} \mathbf{w}(\mathbf{Z}_i, \mathbf{Z}_j)$$

Weighted test statistic:

$$\chi_{\tau}^{2} = \{\mathbf{S} - E_{0}(\mathbf{S})\}' \text{Var}_{0}^{-1}(\mathbf{S}) \{\mathbf{S} - E_{0}(\mathbf{S})\}$$



Weight Function-I: Distance

• Write $\mathbf{Z} = (\mathbf{Z}^{co'}, \mathbf{Z}^{ca'})'$, with \mathbf{Z}^{co} for the continuous covariates and \mathbf{Z}^{ca} for the categorical covariates

$$w(\mathbf{Z}_i, \mathbf{Z}_j; h, q) = W_h(\|\mathbf{Z}_i^{co} - \mathbf{Z}_i^{co}\|)W_q\{I(\mathbf{Z}_i^{ca} \neq \mathbf{Z}_i^{ca})\}$$

For example,

$$W_h(u) = \exp(-u^2/2h^2), \ h > 0,$$

 $W_q(v) = (1-q)I(v=0) + qI(v=1), \ 0 \le q \le 0.5$

Weighted U-statistic (called fixed-(h, q) U-statistic):

$$\mathbf{S}(h,q) = \binom{n}{2}^{-1} \sum_{i < j} D_{ij} \mathbf{F}_{ij} w(\mathbf{Z}_i, \mathbf{Z}_j; h, q)$$



Weight Function-II: Propensity Score

- Propensity score: probability of a unit being assigned to a particular treatment given a set of covariates
- Causal effect analysis: match subjects according to their propensity scores (Rosenbaum and Rubin, 1984)
- Genomic propensity score: $p(\mathbf{z}) = \{p_1(\mathbf{z}), p_2(\mathbf{z})\}', p_c(\mathbf{z}) = P(C = c | \mathbf{Z} = \mathbf{z})$
- Genetic association analysis: match subjects according to their genomic propensity scores
- Weight function:

$$w(\mathbf{Z}_i, \mathbf{Z}_j) = W_h\{\|p(\mathbf{Z}_i) - p(\mathbf{Z}_j)\|\},\$$

with
$$W_h(u) = \exp(-u^2/2h^2), h > 0$$



Asymptotic Distribution: Setting

- Treating the offspring genotype as random
- Conditioning on all phenotypes and parental genotypes (if available)
- Eliminates the assumptions about phenotype distribution, genetic model and parental genotype distribution
- Robust and less prone to population stratification
- In addition, conditioning on covariates

Asymptotic Distribution: Null Hypothesis

• When $n \to \infty$.

$$\operatorname{Var}_{0}^{-1/2} \{ \mathbf{S}(h,q) \} [\mathbf{S}(h,q) - E_{0} \{ \mathbf{S}(h,q) \}] \xrightarrow{\mathcal{D}} N(\mathbf{0}, \mathbf{I}_{p})$$

• Fixed-(h, q) test statistic:

$$\chi^2_{\tau}(h,q) \xrightarrow{\mathcal{D}} \chi^2_p$$

Mean and variance:

$$E_{0}\{\mathbf{S}(h,q)\} = \frac{2}{n-1} \sum_{i=1}^{n} \bar{\mathbf{u}}_{i} E_{0}(C_{i} | M_{i}^{pa}, \mathbf{Z}_{i}),$$

$$\operatorname{Var}_{0}\{\mathbf{S}(h,q)\} = \frac{4}{(n-1)^{2}} \sum_{i=1}^{n} \sum_{j=1}^{n} \bar{\mathbf{u}}_{i} \bar{\mathbf{u}}_{j}' \operatorname{Cov}_{0}(C_{i}, C_{j} | M_{i}^{pa}, M_{j}^{pa}, \mathbf{Z}_{i}, \mathbf{Z}_{j}),$$

with $\bar{\mathbf{u}}_i = n^{-1} \sum_{i=1}^n \mathbf{F}_{ij} w(\mathbf{Z}_i, \mathbf{Z}_j; h, q)$



Asymptotic Distribution: Power

Under the alternative hypothesis,

$$\chi^2_{ au}(h,q) \sim \sum_{i=1}^p e_i \chi^2_1(\phi_i)$$

- $\Delta \mu = \mu_1 \mu_0 \equiv E_1\{\mathbf{S}(h,q)\} E_0\{\mathbf{S}(h,q)\}$
- $\Sigma_0 = \operatorname{Var}_0\{\mathbf{S}(h,q)\}$
- $\Sigma_1 = \operatorname{Var}_1{\{\mathbf{S}(h,q)\}}$
- $e_1 \ge \cdots \ge e_p \ge 0$: eigenvalues of $\Sigma_1^{1/2} \Sigma_0^{-1} \Sigma_1^{1/2}$
- $\Delta \tilde{\mu}_i$: ith component of $\Delta \tilde{\mu} = \mathbf{Q} \mathbf{\Sigma}_1^{-1/2} \Delta \mu$
- \mathbf{Q} : an orthonormal matrix, $\mathbf{Q}\mathbf{\Sigma}_1^{1/2}\mathbf{\Sigma}_0^{-1}\mathbf{\Sigma}_1^{1/2}\mathbf{Q}'=\mathrm{diag}(e_1,\ldots,e_p)$



Factors Determining the Power

- The conditional power \mathcal{P} : $\mathcal{P} = P\left\{\sum_{i=1}^p e_i \chi_1^2(\phi_i) \geq q_{\chi_p^2}(1-\alpha)\right\}$
- Taking a family-based study as an example,

$$\mu_1 = \frac{2}{n-1} \sum_{i=1}^n \bar{\mathbf{u}}_i E(C_i | \mathbf{T}_i, \mathbf{Z}_i, M_i^{pa})$$

$$\Sigma_1 = \frac{4}{(n-1)^2} \sum_{i=1}^n \sum_{j=1}^n \bar{\mathbf{u}}_i \bar{\mathbf{u}}_j' \text{Cov}(C_i, C_j | \mathbf{T}_i, \mathbf{T}_j, \mathbf{Z}_i, \mathbf{Z}_j, M_i^{pa}, M_j^{pa})$$

- By Bayes' theorem, $P(C = c | \mathbf{T}, \mathbf{Z}, M^{pa}) = \frac{P(\mathbf{T} | C = c, \mathbf{Z})P(C = c | M^{pa})}{\sum_{l} P(\mathbf{T} | C = c', \mathbf{Z})P(C = c' | M^{pa})}$
 - Penetrance: $P(\mathbf{T}|C=c,\mathbf{Z})$
 - Allele frequency: $P(C = c|M^{pa})$



Power Approximation

Using the result from Liu et al. (2009), we have

Theorem

$$\mathcal{P} \approx P\{\chi_l^2(\nu) \ge q^*\},$$

where l, ν , and q^* depend on μ_1 and Σ_1 .

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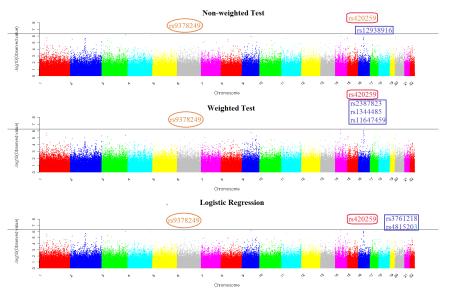


WTCCC Bipolar Disorder Data

- Collected by Wellcome Trust Case-Control Consortium (WTCCC, 2007. Nature)
 - Phenotype: 1998 cases/3004 controls of bipolar disorder
 - Genotype: genotyped by Affymetrix GeneChip 500K arrays
 - Covariates: gender, age at recruitment
- Our method: weighted test using propensity score approach (h = 1)
- Methods for comparison: non-weighted test and logistic regression
- Strong association: p-value $< 5 \times 10^{-7}$; moderate association: $5 \times 10^{-7} < \text{p-value} < 10^{-5}$



Manhattan Plot: Comparison of Three Methods



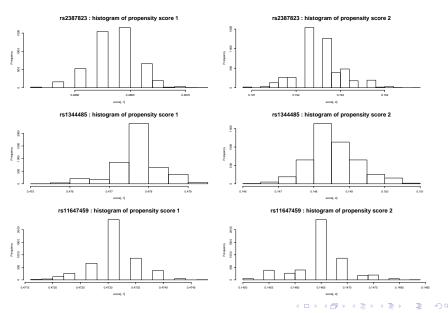
GWAS Results

Chr.	SNP	Position	Non-weighted	Weighted	Logistic Regression
6	rs9378249	31435680	1.21e-8	1.39e-8	1.71e-9
16	rs420259	23541527	8.51e-9	6.59e-8	3.33e-9
16	rs2387823	51445620	2.90e-6	1.30e-7	1.77e-6
16	rs1344485	51469833	1.78e-6	1.79e-7	1.41e-6
16	rs11647459	51473252	2.93e-6	2.76e-7	1.89e-6
17	rs12938916	53221286	4.80e-7	1.11e-6	8.89e-7
20	rs4815603	3720527	3.00e-6	1.42e-5	4.80e-7
20	rs37612181	3724175	1.13e-6	3.27e-6	2.16e-7

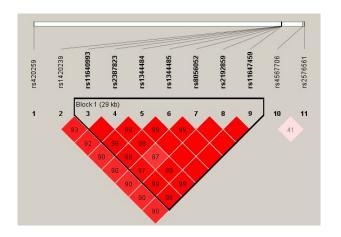
Propensity Scores: Estimation

Chr.	SNP	Gender		Age	Age	
		Coefficient	p-value	Coefficient	p-value	
16	rs2387823	0.0021	0.970	0.0031	0.902	
16	rs1344485	-0.0028	0.959	-0.0049	0.850	
16	rs11647459	0.0004	0.994	0.0038	0.882	

Propensity Scores: Histograms



Significant Region



- 29kb region: 7 strongly linked SNPs
- Haplotype association p-value: 2.64×10^{-7} by weighted test

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Interactions Between rs420259 and New SNPs

Model	Variable	Coefficient	p-value
	rs420259	-0.77415	6.43e-8
(1)	rs9378249	-0.60212	3.88e-8
	$rs420259 \times rs9378249$	0.37602	0.332
	rs420259	-0.63671	1.51e-3
(2)	rs2387823	-0.18834	1.73e-5
	$rs420259 \times rs2387823$	-0.10661	0.561
	rs420259	-0.62866	1.10e-3
(3)	rs1344485	-0.19898	1.14e-5
	$rs420259 \times rs1344485$	-0.10653	0.575
	rs420259	-0.67070	4.43e-4
(4)	rs11647459	-0.19508	1.53e-5
	rs420259 × rs11647459	-0.07443	0.693

Interactions Among New SNPs

Model	Variable	Coefficient	p-value
	rs9378249	-0.49915	1.77e-3
(1)	rs2387823	-0.18455	4.62e-5
	$rs9378249 \times 2387823$	-0.10876	0.461
	rs9378249	-0.49551	1.07e-3
(2)	rs1344485	-0.20266	1.58e-5
	$rs9378249 \times 1344485$	-0.14683	0.344
	rs9378249	-0.48910	1.13e-3
(3)	rs11647459	-0.19580	2.74e-5
	$rs9378249 \times rs11647459$	-0.14960	0.333

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Maximum Weighted Test

- Fixed-(h,q) test: how to choose optimal parameters h and q?
- Choose a grid of h and q values and maximize the weighted test statistic over those choices
- $\{h_1, \ldots, h_{L_1}\}$: pre-specified grid points of h
- $\{q_1,\ldots,q_{L_2}\}$: pre-specified grid points of q

$$\chi^2_{\tau,\max} = \max_{1 \leq l_1 \leq L_1, 1 \leq l_2 \leq L_2} \chi^2_{\tau}(h_{l_1}, q_{l_2})$$

 Approximate the optimal weighting scheme, yielding the strongest association measure



Resampling Approach

- Population-based studies: restricted permutation in Yu et al. (2010)
- Family-based studies: children's genotypes solely determined by their parents' marker alleles, resample the children's genotype by Mendelian laws
- Calculate M resampling test statistics $\tilde{\chi}^2_{\tau \max 1}, \dots, \tilde{\chi}^2_{\tau \max M}$ using Mresampled data
- Resampling p-value: the proportion of the resampling test statistics that exceed our observed test statistic, i.e., $M^{-1} \sum_{m=1}^{M} I(\tilde{\chi}_{\tau,\max,m}^2 \geq \chi_{\tau,\max}^2)$



Asymptotic Distribution: Joint Distribution

Equivalently,

$$\chi^2_{\tau, \max} = \max_{1 \leq l_1 \leq L_1, 1 \leq l_2 \leq L_2} \|\mathbf{R}_{l_1, l_2}\|^2$$

- $\mathbf{R} = \text{Var}_{0D}^{-1/2}(\mathbf{S})\{\mathbf{S} E_0(\mathbf{S})\}\$
- $S = \{S'(h_1, q_1), \dots, S'(h_{L_1}, q_{L_2})\}'$
- $\operatorname{Var}_{0D}(\mathbf{S}) = \operatorname{diag}[\operatorname{Var}_0\{\mathbf{S}(h_1, q_1)\}, \dots, \operatorname{Var}_0\{\mathbf{S}(h_{L_1}, q_{L_2})\}]$: the diagonal blocks of $Var_0(S)$

$$\operatorname{Var}_0^{-1/2}(\mathbf{S})\{\mathbf{S} - E_0(\mathbf{S})\} \xrightarrow{\mathcal{D}} N(\mathbf{0}, \mathbf{I}_{pL_1L_2})$$

• $\tilde{\mathbf{R}} = \text{Var}_{0D}^{-1/2}(\mathbf{S})\text{Var}_{0}^{1/2}(\mathbf{S})\mathbf{G}, \, \mathbf{G} \sim N(\mathbf{0}, \mathbf{I}_{nL_{1}L_{2}})$



Asymptotic Distribution: Uniform Approximation

Theorem

Assume that the eigenvalues of $Var_{0D}(S)$ and $Var_{0}(S)$ are uniformly bounded from both above and below, i.e., there exist two positive numbers c and C such that $c \leq \lambda_{\min} \{ \operatorname{Var}_{0D}(\mathbf{S}) \} \leq \lambda_{\max} \{ \operatorname{Var}_{0D}(\mathbf{S}) \} \leq C$ and $c \leq \lambda_{\min} \{ \text{Var}_0(\mathbf{S}) \} \leq \lambda_{\max} \{ \text{Var}_0(\mathbf{S}) \} \leq C$ uniformly for all n, where λ_{\min} and λ_{\max} denote the smallest and largest eigenvalues respectively. Then for any $x \in \mathbb{R}$, as $n \to \infty$,

$$\sup_{x \in \mathbb{R}} \left| P\left(\chi_{\tau, \max}^2 \le x\right) - P\left(\max_{1 \le l_1 \le l_1, 1 \le l_2 \le l_2} \|\tilde{\mathbf{R}}_{l_1, l_2}\|^2 \le x\right) \right| \to 0.$$

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Aims

- Compare the performance of:
 - Maximum weighted test
 - Non-weighted test
- Compare the performance of:
 - Maximum weighted test
 - Other covariate-adjusted tests

Simulation I: Data Generation

- Generate the parents' disease and marker genotypes via the haplotype frequencies
- Given the parental genotypes, generate the offspring genotype using 1cM between the two loci
- Two covariates are generated: $Z^{co} \sim N(1,2)$
 - Without confounder: $P(Z^{ca} = 1) = 1 P(Z^{ca} = 0) = 0.7$
 - With confounder: $logit{P(Z^{ca} = 1)} = 0.5M^{fa} + 0.5M^{mo}$
- Bivariate ordinal traits are generated according to random effects proportional odds model:

$$logit{P(T^{(j)} \le k)} = \alpha_{j,k} + \beta_g G + \beta_{co} Z^{co} + \beta_{ca} Z^{ca} + U_j,$$

with
$$k = 1, ..., K_i, j = 1, 2$$
, and $(U_1, U_2) \sim N(0, \Sigma)$



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Simulation I: Parameters

- Number of categories: $K_1 = 3$ and $K_2 = 4$
- $(\alpha_{1,1}, \alpha_{1,2}) = (-0.5, -0.3), (\alpha_{2,1}, \alpha_{2,2}, \alpha_{2,3}) = (-0.5, -0.3, -0.1)$
- $\beta_{g} = 2.0$
- $\theta_{ca} = \beta_{ca} = 0, 0.5, 1.0, 1.5, 2.0$
- The grid of h is $\{C_1(C_2/C_1)^{(l_1/(L_1-1))}: l_1=0,\ldots,L_1-1\}$, with $C_1 = 0.05, C_2 = 10, L_1 = 8$
- The grid of q is $\{0.5l_2/(L_2-1): l_2=0,\ldots,L_2-1\}$, with $L_2=5$



Type I Error of Maximum Weighted Test

		Significance Level			
Confounder	n	$\alpha = 0.05$	$\alpha = 0.01$	$\alpha = 0.001$	
No	200	0.0466	0.0090	0.0006	
	400	0.0512	0.0097	0.0010	
Yes	200	0.0469	0.0084	0.0007	
	400	0.0462	0.0090	0.0011	

Power Comparison: Without Confounder

			Covariate effect				
n	α	Method	0.0	0.5	1.0	1.5	2.0
200	0.05	Weighted	0.681	0.521	0.372	0.275	0.222
		Non-weighted	0.726	0.522	0.306	0.189	0.135
	0.01	Weighted	0.432	0.281	0.161	0.099	0.071
		Non-weighted	0.491	0.283	0.128	0.064	0.041
	0.001	Weighted	0.160	0.082	0.036	0.017	0.011
		Non-weighted	0.223	0.097	0.028	0.011	0.006
400	0.05	Weighted	0.948	0.848	0.685	0.551	0.448
		Non-weighted	0.960	0.838	0.565	0.348	0.233
	0.01	Weighted	0.846	0.658	0.441	0.297	0.213
		Non-weighted	0.877	0.643	0.321	0.154	0.084
	0.001	Weighted	0.563	0.337	0.164	0.091	0.054
		Non-weighted	0.671	0.361	0.115	0.040	0.018

Power Comparison: With Confounder

-			Covariate effect				
n	α	Method	0.0	0.5	1.0	1.5	2.0
200	0.05	Weighted	0.695	0.557	0.405	0.310	0.250
		Non-weighted	0.728	0.528	0.308	0.194	0.139
	0.01	Weighted	0.452	0.305	0.181	0.120	0.087
		Non-weighted	0.495	0.288	0.129	0.066	0.041
	0.001	Weighted	0.165	0.090	0.046	0.024	0.015
		Non-weighted	0.224	0.095	0.032	0.011	0.006
400	0.05	Weighted	0.951	0.867	0.718	0.593	0.493
		Non-weighted	0.961	0.834	0.573	0.363	0.251
	0.01	Weighted	0.854	0.682	0.483	0.345	0.250
		Non-weighted	0.875	0.645	0.332	0.170	0.094
	0.001	Weighted	0.572	0.355	0.196	0.111	0.069
		Non-weighted	0.665	0.364	0.129	0.044	0.020

Simulation II: Other Covariate-Adjusted Methods

- FBAT-GEE (Lange et al. 2003) adjusting for covariates:
 - Fit the regression model $g(E[T^{(j)}]) = \alpha_i + \lambda_i' \mathbf{Z}$, with $g(\cdot)$ an appropriate link function
 - Replace the original traits $T^{(j)}$ with the residuals $T^{(j)} g^{-1}(\alpha_i + \lambda_i' \mathbf{Z})$ in the FBAT-GEE test statistic
- Ordinal trait test (Wang, Ye and Zhang, 2006):
 - Deal with a single ordinal trait at a time
 - Apply the Bonferroni correction for multiple trait testing

Simulation II: Data Generation

- Continuous covariate: $Z^{co} \sim N(1,2)$
- Bivariate quantitative traits:

$$Y^{(j)} = \mu + \beta_g G + \beta_{co} Z^{co} + \epsilon_j, \ j = 1, 2,$$

with $(\epsilon_1, \epsilon_2)' \sim 2\phi_2(\mathbf{x}; \mathbf{\Sigma})\Phi(\boldsymbol{\alpha}'\mathbf{x}), \mathbf{x} \in \mathbb{R}^2$ (bivariate skew normal distribution)

- Bivariate ordinal traits: discretizing quantitative traits by (50%, 67%) and (33%, 54%, 75%) percentiles
- $\alpha = (5,5)$ and $\Sigma = \begin{pmatrix} 1 & 0.25 \\ 0.25 & 1 \end{pmatrix}$
- $\mu = 0, \beta_{\sigma} = \beta_{co} = 0.8$



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Power Comparison

		0.			
		Significance Level			
n	Method	$\alpha = 0.05$	$\alpha = 0.01$	$\alpha = 0.001$	
200	$\chi^2_{ au, \mathrm{max}}$	0.640	0.381	0.134	
	FBAT-GEE	0.608	0.355	0.137	
	Wang et al.'s Test	0.448	0.236	0.081	
400	$\chi^2_{ au, \mathrm{max}}$	0.930	0.815	0.518	
	FBAT-GEE	0.902	0.758	0.499	
	Wang et al.'s Test	0.775	0.590	0.320	
600	$\chi^2_{ au, ext{max}}$	0.991	0.961	0.817	
	FBAT-GEE	0.982	0.938	0.787	
	Wang et al.'s Test	0.925	0.807	0.585	

Outline

- - Generalized Kendall's Tau
 - Asymptotic Distribution and Power
 - Application to WTCCC Bipolar Disorder Data
- - Asymptotic Distribution
- **Analysis of Comorbidity**
 - Application to COGA Family Data
 - Application to SAGE GWAS Data



Collaborative Studies on Genetics of Alcoholism

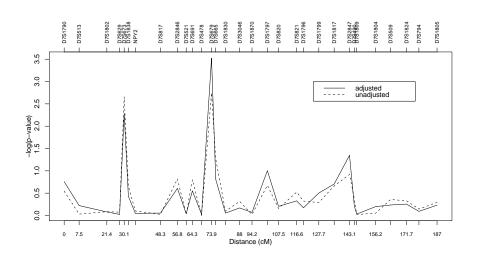
A large scale study to map alcohol dependence susceptible genes



COGA Data

- The data include 143 families with a total of 1,614 individuals
- Multiple Traits:
 - ALDX1 (the severity of the alcohol dependence): pure unaffected, never drunk, unaffected with some symptoms, and affected
 - MaxDrink (maximum number of drinks in a 24 hour period): 0-9, 10-19, 20-29, and more than 30 drinks
 - TimeDrink (spent so much time drinking, had little time for anything else): "no", "yes and lasted less than a month", and "yes and lasted for one month or longer"
- Genotypes: markers on chromosome 7
- Covariates: age at interview and gender

Results





Outline

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Study of Addiction: Genetics and Environment (SAGE)

- The data were from SAGE (Bierut et al. 2010), a case-control study of mostly unrelated individuals aimed at identifying genetic associations for addiction.
- We included 4,121 subjects for whom the addiction to the six categories of substances and genomewide SNP data (ILLUMINA Human 1M platform) were available.
- We defined the outcome as to whether a subject was addicted to substances in at least two of the six addiction categories (nicotine, alcohol, marijuana, cocaine, opiates or others).

Peak SNPs in PKNOX2 in White Women

SNP	P-value	Odds Ratio
rs1426153 (G)	1.84E-06	1.66
rs11220015(A)	1.97E-06	1.65
rs11602925(G)	1.24E-06	1.67
rs750338(C)	4.22E-07	1.63
rs12273605(T)	3.83E-06	1.71
rs10893365(C)	2.27E-07	1.72
rs10893366(T)	6.87E-07	1.70
rs12284594(G)	7.13E-08	1.77

Peak SNPs in PKNOX2 in White Women for Individual Substances

SNP	Nicotine	Alcohol	Marijuana	Cocaine	Opiates
rs1426153 (G)	0.0159	5.75E-5	7E-4	3E-4	0.0113
rs11220015(A)	0.0163	6.86E-5	0.0010	3E-4	0.0037
rs11602925(G)	0.0136	4.24E-5	7E-4	3E-4	0.0059
rs750338(C)	0.0491	4.26E-5	0.0013	2E-4	0.0112
rs12273605(T)	0.0921	3E-4	3.53E-5	1E-4	0.0680
rs10893365(C)	0.0411	1.72E-5	8.58E-6	2.91E-5	0.0699
rs10893366(T)	0.0621	1.37E-5	8.80E-6	8.63E-5	0.0905
rs12284594(G)	0.0239	1.97E-6	8.54E-6	4.39E-5	0.0533

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Result

- PKNOX2 is a novel TALE homeodomain-encoding gene, located at 11q24 in humans
- It functions as a nuclear transcription factor indicated by its structure and sub-cellular localization
- One of the cis-regulated genes for alcohol addiction in mice (Mulligan et al. 2006)
- Confirmed by multiple studies

Conclusions: Method

- Developed a nonparametric weighted test to adjust for covariates that accommodates multiple traits
- Provided its asymptotic distribution and analytical power calculation
- Refined the weighted test by proposing the idea of maximum weighting over the grid points of parameters
- Proposed an asymptotic approach to assess its significance

Conclusions: Application

- WTCCC bipolar disorder data: not only confirmed SNP rs420259 on Chromosome 16 reported by the WTCCC (2007), but also identified two regions (rs9378249 on chr 6; rs12938916 on chr 17) at the genome-wide significance level
- The identified haplotype block is near the RPGRIP1L gene that was reported to be associated with bipolar disorder (O'Donovan et al., 2008; Riley et al., 2009)
- COGA data: confirmed and strengthened the top signal; provided evidences for the advantage of maximum weighted test over non-weighted test
- SAGE data: identified PKNOX2 for addiction, which has been confirmed by other studies

Other Ongoing/Future Work

- Incorporating genetic prior information into a current study
- Genetic association analysis for rare variants
- Nonparametric test for gene-environment interactions
- Genetic test for multiple trait covariance structure

Acknowledgment

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- The COGA data were provided by COGA
- The views expressed here are those of the authors.

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 $\{M_i|y_i\} = \frac{1}{P\{y_i\}} \prod_j [P\{y_{ij}|c_{ij} = 0\}P]$

 $= \frac{P\{M_i\}}{P\{y_i\}} \prod_{j} [\pi(\beta; y_{ij}, 0) P\{a\}]$

 $\frac{P(y_i)}{P(y_i)} \prod_{i} (\pi(\mathbf{B}, y_i, 0)) P(dd(M_{\mathbf{B}}) + \pi(\mathbf{B}, y_i))$ $= \frac{P(\Delta t_i)}{P(y_i)} \prod_{i} (\pi(\mathbf{B}, y_i, 0)) P(dd(M_{\mathbf{B}}) + \pi(\mathbf{B}, y_i))$



3; k, ϵ) = $P\{y_{\theta} = k | \epsilon_{\theta} = \epsilon\}$ = $\gamma(\beta)$; K = 1, $\gamma(\beta)$, 0, ϵ) = 0, and $\gamma(\beta)$, K = 1.

$$P\{y_i\} = \prod_i [P\{y_{ij}|\,c_{ij}=0\}I$$

$$=\prod [\pi(\beta; y_{ij}, 0)P\{$$

ale to see that $(\partial/\partial B)\pi(B; k, \epsilon) =$

$$\operatorname{og}(P\{M_i|y_i\}) = -\frac{\partial}{\partial \beta}\operatorname{log}(P\{y_i\})$$

 $+\sum \frac{\partial}{\partial \gamma \operatorname{log}(B)}$

be null by notheris that B = 0, we

$$\frac{\partial}{\partial \boldsymbol{\beta}} \mathrm{log}[\pi(\boldsymbol{\beta};\; y_{ij},\; \boldsymbol{0}) P\{dd|M_{ij}$$

$$\frac{\partial}{\partial a} \log P\{y_l\}|_{a=0} = \sum [1$$

oniones we drop the two irrelant

$$g(P\{M_i|y_i\})|_{\beta=0} = \sum_j [1 - \gamma(y_{ij}) - \gamma]$$

= $\sum_j \frac{1 - \gamma(y_{ij}) - \gamma}{P^{f,M}}$

e coefficient of linkage disequilibr



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